

MATHEMATICS FORMULA BOOK

# CLASS 11

Complete Formula & Concept Book (CBSE/NCERT)

**Covers:** Complete syllabus formulas

**Use:** Quick revision & exam preparation

**Format:** Chapter-wise formula reference

All formulas, identities, theorems & results in one place

## 1 Sets

Union

$$A \cup B = \{x : x \in A \text{ or } x \in B\}$$

Intersection

$$A \cap B = \{x : x \in A \text{ and } x \in B\}$$

Difference

$$A - B = \{x : x \in A, x \notin B\}$$

Complement

$$A' = U - A$$

De Morgan's Laws

$$(A \cup B)' = A' \cap B'; (A \cap B)' = A' \cup B'$$

$n(A \cup B)$

$$n(A) + n(B) - n(A \cap B)$$

$n(A \cup B \cup C)$

$$n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(A \cap C) + n(A \cap B \cap C)$$

Power Set Cardinality

$$|P(A)| = 2^n$$

## 2 Relations and Functions

Number of Relations

$$2^{mn} \text{ from set of } m \text{ to set of } n$$

Domain, Codomain, Range

$$\text{Range} \subseteq \text{Codomain}$$

## 3 Trigonometric Functions

Radian Measure

$$\pi \text{ radians} = 180^\circ$$

Arc Length

$$l = r\theta$$

### Fundamental Identities

Identity 1

$$\sin^2 x + \cos^2 x = 1$$

Identity 2

$$1 + \tan^2 x = \sec^2 x$$

Identity 3

$$1 + \cot^2 x = \operatorname{cosec}^2 x$$

### Sum & Difference Formulas

| Formula     | Expression                                |
|-------------|-------------------------------------------|
| $\sin(x+y)$ | $\sin x \cos y + \cos x \sin y$           |
| $\sin(x-y)$ | $\sin x \cos y - \cos x \sin y$           |
| $\cos(x+y)$ | $\cos x \cos y - \sin x \sin y$           |
| $\cos(x-y)$ | $\cos x \cos y + \sin x \sin y$           |
| $\tan(x+y)$ | $(\tan x + \tan y) / (1 - \tan x \tan y)$ |
| $\tan(x-y)$ | $(\tan x - \tan y) / (1 + \tan x \tan y)$ |

### Double & Triple Angle

| Formula   | Expression                                        |
|-----------|---------------------------------------------------|
| $\sin 2x$ | $2 \sin x \cos x$                                 |
| $\cos 2x$ | $\cos^2x - \sin^2x = 2\cos^2x - 1 = 1 - 2\sin^2x$ |
| $\tan 2x$ | $2\tan x / (1 - \tan^2x)$                         |
| $\sin 3x$ | $3\sin x - 4\sin^3x$                              |
| $\cos 3x$ | $4\cos^3x - 3\cos x$                              |

### Sum-to-Product

|                   |                                  |
|-------------------|----------------------------------|
| $\sin A + \sin B$ | $2 \sin[(A+B)/2] \cos[(A-B)/2]$  |
| $\sin A - \sin B$ | $2 \cos[(A+B)/2] \sin[(A-B)/2]$  |
| $\cos A + \cos B$ | $2 \cos[(A+B)/2] \cos[(A-B)/2]$  |
| $\cos A - \cos B$ | $-2 \sin[(A+B)/2] \sin[(A-B)/2]$ |

### Sine & Cosine Rule (Triangle)

|                                                                 |
|-----------------------------------------------------------------|
| Sine Rule<br><b><math>a/\sin A = b/\sin B = c/\sin C</math></b> |
| Cosine Rule<br><b><math>\cos A = (b^2+c^2-a^2)/2bc</math></b>   |

## 4 Principle of Mathematical Induction

- Base step: verify P(1) is true
- Inductive step: assume P(k), prove P(k+1)

## 5 Complex Numbers and Quadratic Equations

|                                                                     |
|---------------------------------------------------------------------|
| Imaginary Unit<br><b><math>i^2 = -1</math></b>                      |
| Complex Number<br><b><math>z = a + ib</math></b>                    |
| Modulus<br><b><math> z  = \sqrt{a^2+b^2}</math></b>                 |
| Conjugate<br><b><math>\bar{z} = a - ib</math></b>                   |
| Argand Form<br><b><math>z = r(\cos\theta + i \sin\theta)</math></b> |
| Powers of i<br><b><math>i^1=i, i^2=-1, i^3=-i, i^4=1</math></b>     |

## 6 Linear Inequalities

- Multiplying/dividing inequality by negative number reverses inequality sign
- Graphical solution: shaded common region

## 7 Permutations and Combinations

|                                                                          |
|--------------------------------------------------------------------------|
| Factorial<br><b><math>n! = n \times (n-1) \times ... \times 1</math></b> |
| Permutation<br><b><math>{}^nP_r = n!/(n-r)!</math></b>                   |
| Combination<br><b><math>{}^nC_r = n!/[r!(n-r)!]</math></b>               |

Relation  
 ${}^n\text{P}_r = r! \times {}^n\text{C}_r$

Circular Permutation  
 $(n-1)!$

## 8 Binomial Theorem

Binomial Expansion  
 $(x+y)^n = \sum {}^nC_r x^{n-r} y^r$

General Term  
 $T_{r+1} = {}^nC_r x^{n-r} y^r$

Middle Term (n even)  
 $(n/2 + 1)\text{th term}$

## 9 Sequences and Series

### Arithmetic Progression (AP)

nth Term  
 $a_n = a + (n-1)d$

Sum of n Terms  
 $S_n = n/2[2a + (n-1)d]$

Arithmetic Mean  
 $A = (a+b)/2$

### Geometric Progression (GP)

nth Term  
 $a_n = ar^{n-1}$

Sum of n Terms  
 $S_n = a(r^n - 1)/(r - 1), r \neq 1$

Sum to Infinity  
 $S_\infty = a/(1-r), |r| < 1$

Geometric Mean  
 $G = \sqrt{ab}$

Sum of Squares ( $1^2 + 2^2 + \dots + n^2$ )  
 $n(n+1)(2n+1)/6$

Sum of Cubes ( $1^3 + 2^3 + \dots + n^3$ )  
 $[n(n+1)/2]^2$

## 10 Straight Lines

Slope (2 points)  
 $m = (y_2 - y_1)/(x_2 - x_1)$

Slope-Intercept Form  
 $y = mx + c$

Point-Slope Form  
 $y - y_1 = m(x - x_1)$

Two-Point Form  
 $y - y_1 = [(y_2 - y_1)/(x_2 - x_1)](x - x_1)$

Intercept Form  
 $x/a + y/b = 1$

Normal Form

**$x \cos \omega + y \sin \omega = p$**

Distance of Point from Line

**$|Ax_1 + By_1 + C|/\sqrt{A^2 + B^2}$**

Distance Between Parallel Lines

**$|C_1 - C_2|/\sqrt{A^2 + B^2}$**

Angle Between Two Lines

**$\tan \theta = |(m_1 - m_2)/(1 + m_1 m_2)|$**

**11 Conic Sections**

| Conic | Standard Equation |
|-------|-------------------|
|-------|-------------------|

|        |                   |
|--------|-------------------|
| Circle | $x^2 + y^2 = r^2$ |
|--------|-------------------|

|          |             |
|----------|-------------|
| Parabola | $y^2 = 4ax$ |
|----------|-------------|

|         |                                                  |
|---------|--------------------------------------------------|
| Ellipse | $x^2/a^2 + y^2/b^2 = 1 \text{ (} a > b \text{)}$ |
|---------|--------------------------------------------------|

|           |                         |
|-----------|-------------------------|
| Hyperbola | $x^2/a^2 - y^2/b^2 = 1$ |
|-----------|-------------------------|

Eccentricity (Ellipse)

**$e = \sqrt{1 - b^2/a^2}$**

Eccentricity (Hyperbola)

**$e = \sqrt{1 + b^2/a^2}$**

Latus Rectum (Parabola)

**$4a$**

**12 Introduction to 3D Geometry**

Distance Formula (3D)

**$\sqrt{[(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2]}$**

Section Formula (3D)

**$[(mx_2 + nx_1)/(m + n), (my_2 + ny_1)/(m + n), (mz_2 + nz_1)/(m + n)]$**

**13 Limits and Derivatives**

Derivative Definition

**$f'(x) = \lim_{h \rightarrow 0} [f(x+h) - f(x)]/h$**

d/dx ( $x^n$ )

**$n \cdot x^{n-1}$**

d/dx (sin x)

**$\cos x$**

d/dx (cos x)

**$-\sin x$**

d/dx ( $e^x$ )

**$e^x$**

d/dx (ln x)

**$1/x$**

Product Rule

**$(uv)' = u'v + uv'$**

Quotient Rule

**$(u/v)' = (u'v - uv')/v^2$**

$\lim_{x \rightarrow 0} \sin x/x$

**$= 1$**

## 14 Statistics

Mean Deviation about Mean

$$\Sigma |x_i - \bar{x}| / n$$

Variance

$$\sigma^2 = \Sigma (x_i - \bar{x})^2 / n$$

Standard Deviation

$$\sigma = \sqrt{\text{Variance}}$$

Coefficient of Variation

$$(\sigma / \bar{x}) \times 100$$

## 15 Probability

$P(A \cup B)$

$$P(A) + P(B) - P(A \cap B)$$

Mutually Exclusive

$$P(A \cap B) = 0$$

Complementary

$$P(A') = 1 - P(A)$$